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Bio-inspired self-folding strategy to break the trade-off between strength and ductility in carbon-nanoarchitected materials

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Graphene possesses extraordinary mechanical, electronic, and thermal properties, thus making it one of the most promising building blocks for constructing macroscopic high performance and multifunctional materials. However, the common material strength–ductility paradox also appears in the carbon-nanoarchitected materials and some of the key mechanical performance, for example, the tensile strength of graphene-based materials, are still far lower than that of graphene. Inspired by the exceptional mechanical performance of silk protein benefiting from the conformations of folded structures as well as their transitions, this work proposed a topological strategy to yield graphene-based materials with ultrahigh ductility while maintaining decent tensile strength by self-folding graphene sheets. This drastically improved mechanical performance of graphene-based materials is attributed to the exploitation of shearing, sliding, and unfolding deformation at the self-folded interface. Molecular dynamics simulations show that both modulating self-folded length and engineering interface interaction can effectively control the strength, ductility, and the ductile failure of van der Waals interfaces among the self-folded structures, where interfacial shearing, sliding, and unfolding open channels to dissipate mechanical energy. Based on the insights into the atomic-scale deformation by molecular dynamics simulations, the underlying mechanism of deformation and failure of these materials is finally discussed with a continuum mechanics-based model. Our findings bring perceptive insights into the microstructure design of strong-yet-ductile materials for load-bearing engineering applications.

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INTRODUCTION

Graphene has attracted considerable attention owing to its excellent thermal,¹ electronic², and mechanical³ properties. The tensile stiffness, tensile strength, and fracture strain of graphene can reach as high as 1 TPa, 120 GPa and 15%, respectively,³ making it a promising candidate for constructing macroscopic materials that inherit the superior mechanical properties of this carbon nanostructure. In the past decades, considerable theoretical, computational, and experimental works have been devoted to the rational design of multi-layer graphene assemblies. On the theoretical and computational sides, studies have been conducted on the theoretical modeling and computational simulations of multi-layer graphene assemblies. Considering the in-plane tensile deformation of the building blocks, Liu et al.⁴ and Wei et al.⁵ proposed the shear-lag model for the layered/bundled assemblies of carbon nanostructures, and recently He et al.⁶ generalized this model by introducing elastic-plastic interface. By virtue of this shear-lag model, the overall mechanical response and structural deformation of multi-layer graphene assemblies can be correlated for material analysis and design.^{4,6–8} Subsequently, Ruiz et al.⁹ developed a coarse-grained molecular dynamics (CGMD) model of multi-layer graphene assemblies. By using this CGMD model, Xia et al.¹⁰ investigated the mechanical behaviors of multi-layer graphene assemblies and found that critical length scales and strain localization govern the mechanical behaviors of these assemblies. Meanwhile, the CGMD model was also applied to design multi-layer graphene assemblies for enhanced toughness.¹¹ Furthermore, Meng et al.¹² conducted ballistic impact simulations of multi-layer graphene assemblies and demonstrated

that a spalling-like failure by cylindrical projectiles deteriorates the ballistic performance of these materials. On the experimental side, recent studies used various methods, such as nanoindentation,¹³ in situ tensile test,¹⁴ and projectile penetration¹⁵ to characterize the mechanical behaviors of multi-layer graphene assemblies. Combining nanomechanical experiments and CGMD simulations, Wei et al.¹³ found that both the tensile strength and Young's modulus of multi-layer graphene assemblies decrease with increasing thickness and elucidated the mechanisms therein. Lee et al.¹⁵ studied the dynamic mechanical behaviors of multi-layer graphene assemblies by supersonic projectile penetration and demonstrated that their energy dissipation capacity can suppress conventional protective materials. Recently, Li et al.¹⁴ characterized the in-plane fracture behaviors of multi-layer graphene assemblies under tensile loading by using in situ electron microscopy and found that the fracture strength of multi-layer graphene assemblies decreases as the thickness increases. Additionally noted that considerable defects in the building blocks of graphene sheets have been characterized by experiments,¹⁶ and the load transfer through the van der Waals interfaces of graphene assemblies is weak,⁸ which limits the mechanical performance of graphene-based materials. To enhance the mechanical properties of graphene-based materials, two main strategies including improving the quality of the building blocks and modifying the interface interaction between building blocks were developed.¹⁷ The first strategy includes developing and modulating the intrinsic chemical structure of graphene building blocks.^{18–31} For example, Zhang et al.³⁰ prepared graphene films with a tensile strength of 453 MPa by

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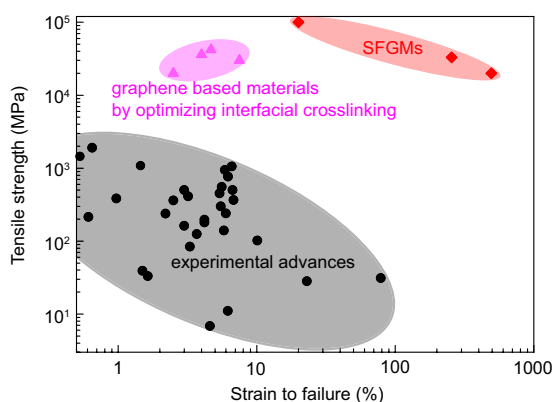


Fig. 1 Material strength–ductility paradox. Tensile strength and strain to failure of graphene-based materials reported in experimental and computational studies (Supplementary Table 1). The graphene-based materials fabricated in experiments exhibit multi-level structures and considerable defects, which are difficult to fairly compare with that from computational studies. Herein, SFGMs set a reference limit on the strength–ductility of graphene-based materials.

modifying the chemical structures of graphene building blocks. The second strategy is interfacial engineering, including hydrogen bonding,³² ionic bonding,^{33–35} π – π bonding,^{36–38} covalent bonding,^{39–42} and synergistic interactions,^{17,43,44} which can be integrated into the graphene-based materials and thus enable the efficient load transfer among the building blocks. For example, Wan et al.⁴⁴ fabricated graphene films with a tensile strength of 945 MPa by successive application of the optimized ratio of π – π bonding and covalent bonding agents. However, after decades of extensive work, some of the key mechanical performance are far lower than their ideal values; for example, the tensile strength of graphene-based materials (Supplementary Table 1) is still far lower than that of their building blocks (about 100 GPa). Graphene-based materials could be processed to exhibit high ductility but usually at the expense of substantial loss of strength. For example, Xiao et al.⁴⁵ fabricated graphene films with rich hierarchical wrinkles and folds, which have a rubber-like mechanical behavior with remarkably large fracture strain of 23% but the tensile strength of only about 30 MPa. This strength–ductility paradox emerging in graphene-based materials (Fig. 1) largely limits their wide uses in load-bearing applications. Therefore, the rational design of the microstructures in graphene-based materials that breaks strength–ductility trade-off is highly desirable.

Evolved over billions of years, biomaterials provide a source of inspiration in designing high performance and multifunctional materials. A large number of biomaterials, for example, natural silk, feature exceptional mechanical properties including high strength and large extensibility, resulting from their folded structures of β -sheets. As shown in Fig. 2a, b, the β -sheet consisting of β -strands is one of the secondary elementary building blocks of protein.⁴⁶ Unlike most common polymers, protein molecules consisting of one or more long chains of amino acid residues adopt specific three-dimensional conformations (called the native folds) that have a large number of favorable interactions within the protein. The self-folded structures of β -sheets (referred to conformations) and changes between them (called conformation transitions) endow the protein with fascinating mechanical properties and thus fulfill specific biological functions.^{47,48}

In this work, inspired by the self-folded structures that endow protein with fascinating mechanical performance, we developed a self-folded topological strategy to enhance the mechanical properties of graphene-based materials by assembling graphene into self-folded graphene-based materials (SFGMs, Fig. 2c, d). The representative elementary building unit of SFGMs is similar

to the simple but intriguing self-assembled graphene observed in recent experiments and simulations: the spontaneous self-tearing and peeling off towards the formation of a micrometer-size folded graphene.^{49–51} Molecular dynamics (MD) simulations of the deformation and failure of SFGMs were performed, which indicate that interfacial shearing, sliding, and unfolding among adjacent graphene interface dissipate mechanical energy and thus endow the films with exceptional strength–ductility synergy. To optimize the mechanical performance, a wide range of interface interaction and self-folded length of SFGMs were exploited. With the understanding of the underlying mechanism discussed by continuum mechanics-based model, optimal interface interaction and self-folded length of SFGMs for mechanical enhancement were identified based on our simulation results.

RESULTS AND DISCUSSION

Typical mechanical behaviors of SFGMs

The representative volume element (RVE) of SFGMs before and after tension is illustrated in Fig. 2 and Supplementary Fig. 1, where the h_0 , L , and L_0 are the interlayer spacing between folded layers, total length, and self-folded length of the RVE, respectively. We first investigate the stability of SFGMs by performing simulations of SFGMs having different self-folded lengths (L_0) and interface interactions (ϵ) under the temperature of 300 K for 1 ns (see Methods for details). It demonstrates that the stability of SFGMs increases with the increasing of L_0 and ϵ (Fig. 3), indicating a controlled stability by modulating the geometrical and mechanical parameters of SFGMs. Subsequently, we investigate the deformation and failure of a typical SFGM with L_0 of 38.4 nm and ϵ of $10\epsilon_0$. The strain–stress curve is shown in Fig. 4a, where the nominal strain (ϵ , the change of length divided by the original length) and nominal stress (σ , the tensile force divided by the original cross-sectional area) are adopted. The simulation cartoons and snapshots of SFGMs under tension are shown in Fig. 4b and Supplementary Fig. 2, respectively. Herein the stretching process is divided into four stages: (I) The first stage: from point A to point B. The stress arises rapidly with the increasing of strain until the first peak stress (σ_1), named as unfolding strength. In this stage, the increasing tensile loads applied in the overall structure are transferred into the shear deformation of self-folded interface. (II) The second stage: from point B to point C. First, there is a slight drop in stress following point B, and this drop is similar to that of multi-layer graphene assemblies in the study of Xia et al.,¹⁰ which is attributed to the transition from static friction to dynamic friction. Subsequently, the stress changes slightly, and the average stress in the plateau regime (Fig. 4a) is named as plateau stress (σ_p). Afterwards, the stress decreases with the strain increasing since the interface sliding of SFGMs significantly reduces the self-folded length L_0 , indicating there is a negative-stiffness region of SFGMs in this stage. The elongation of the material in the range of negative stiffness would jump if it is loaded using constant force instead of constant displacement. Despite the fact that it still dissipates mechanical energy in this range, a more rational design of SFGMs should be developed to avoid or delay the catastrophic moment of the material for practical applications. Future efforts should be directed, but not limited, at introducing multimodal and self-healable interfaces to enable strong and tough SFGMs.⁷ For engineering applications, the stiffness could be modulated by introducing other microstructures, for example, interlayer cross-links of different lengths. Additionally, the strain-rate effect observed in the simulations (Supplementary Fig. 3) can be expected to help SFGMs to damp the deformations during dynamical loading. (III) The third stage: from point C to point D. As the strain continues to increase, the stress decreases abruptly as a

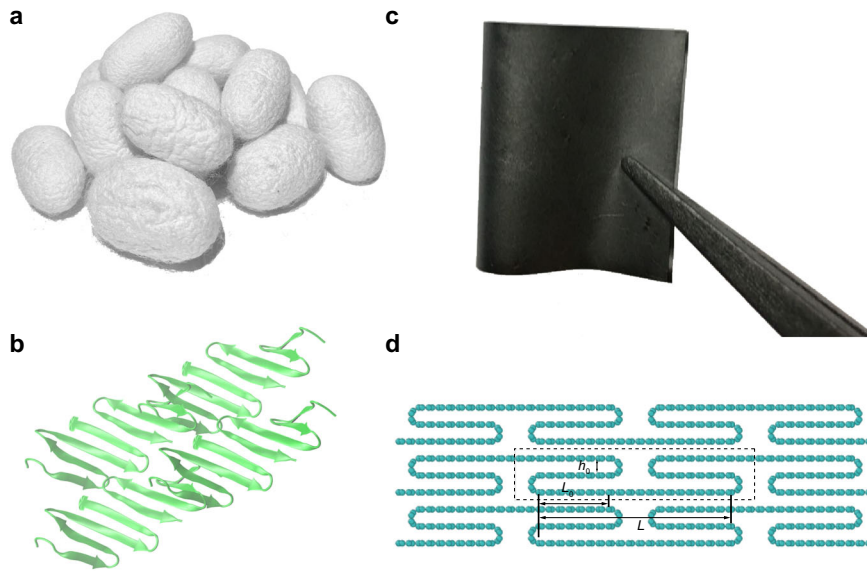


Fig. 2 Natural silk and the graphene-based materials. **a** Optical image of silk and **b** illustration of folded β -sheets. **c** Optical image of graphene-based materials and **d** illustration of SFGM structure.

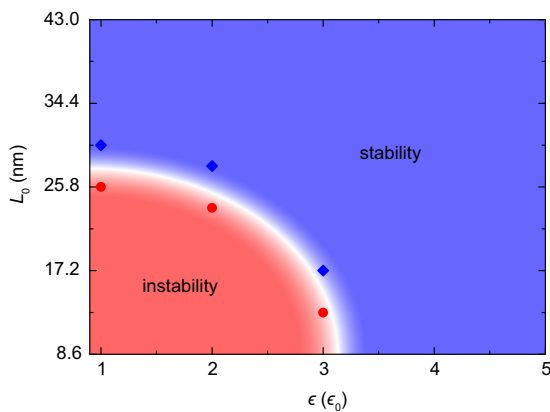


Fig. 3 Effects of the geometrical (L_0) and mechanical (ϵ) parameters on the stability of SFGMs under the temperature of 300 K.

critical transition from the folded multilayers to unfolded monolayer occurs. (IV) The fourth stage: from point D to point E. This stage shows the mechanical behavior of completely unfolded SFGM. It is similar to that of monolayer graphene (tensile strength of about 100 GPa and thickness of about 0.34 nm), where the second peak stress (tensile strength, σ_2) is observed at the failure of this unfolded monolayer. The original thickness of SFGMs with three-folded layers is about three times of that of pristine graphene. Hence, the nominal tensile strength can be predicted as about $100/3 = 33$ GPa, which is also observed in the simulation results (Fig. 4a). Additionally, the MD simulations demonstrate that the fracture strain of SFGMs could reach as high as 258%.

Effect of interface interaction on the mechanical behaviors of SFGMs

To investigate the effect of different levels of interface interaction including hydrogen bonding,³² ionic bonding,^{33–35} π - π bonding,^{36–38} covalent bonding,^{39–42} and synergistic interactions^{17,43,44} that can be integrated in experiments, simulations of SFGMs with

a wide range of interface interaction were performed by modifying the Lennard–Jones potential well of AIREBO potential (ϵ). To modulate the interface interaction of SFGMs, the value of ϵ is modified as 1–30 times of the pristine value (ϵ_0), corresponding to the interlayer shear moduli of 0.32–10.62 GPa benchmarked in Supplementary Fig. 4. The strain–stress curves of SFGMs with L_0 of 38.4 nm and ϵ from $1\epsilon_0$ to $30\epsilon_0$ are studied by MD simulations in Fig. 5a, and the key mechanical properties including σ_p and E_p (strain energy density, the area under the strain–stress curve before fracture) are summarized in Fig. 5b. Both σ_p and E_p of SFGMs increase with the increasing of ϵ from $1\epsilon_0$ to $25\epsilon_0$ and then almost reach their maximum values near ϵ of $25\epsilon_0$. Afterwards, σ_p and E_p suddenly drop at ϵ of $30\epsilon_0$, since the excessive interface interaction leads to the premature intralayer failure of SFGMs before sliding. Herein the interface interaction for maximizing σ_p and E_p is defined as the optimal value. Additionally, remarked here that SFGMs with higher ϵ prefer to prematurely unfold one side because of the strain localization therein, which corresponds to the dip in stage II of the strain–stress curve (Fig. 5a, Supplementary Fig. 5).

Effect of the self-folded length on the mechanical behaviors of SFGMs

To investigate the effect of self-folded length (L_0) on the deformation and failure of SFGMs, we conducted simulations of SFGMs with L_0 of 38.4, 51.2, 64.0, and 76.8 nm, respectively. It is found that Y_{eff} , σ_1 , σ_p , and E_p first increase and then converge to limited values with the increasing of L_0 (Fig. 5, Supplementary Fig. 6a, b). Since σ_1 closely correlates with σ_p and E_p , which determines the level of load bearing of SFGMs, the critical length of L_0 as σ_1 converges to a value is defined as the optimal self-folded length. We further find that the optimal self-folded length decreases with the increasing of ϵ (Supplementary Fig. 7).

As discussed previously, we have optimized the interfacial and geometrical parameters to maximize the mechanical performance of SFGMs (Fig. 5). The results show significantly enhanced mechanical properties of SFGMs (σ_1 , σ_p , and E_p) by modulating the interfacial and geometrical parameters of SFGMs (ϵ and L_0). Based on these improvements, SFGMs are highly promising for uses in engineering applications.

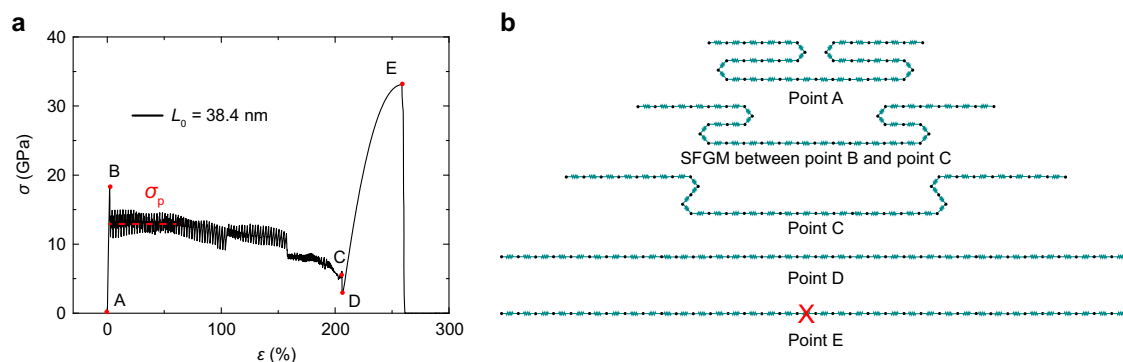


Fig. 4 Typical mechanical behaviors of SFGM. a Strain–stress curve of SFGM that can be divided into different stages. **b** Cartoons of SFGMs under tension. The snapshots of the MD simulation can be found in Supplementary Fig. 2.

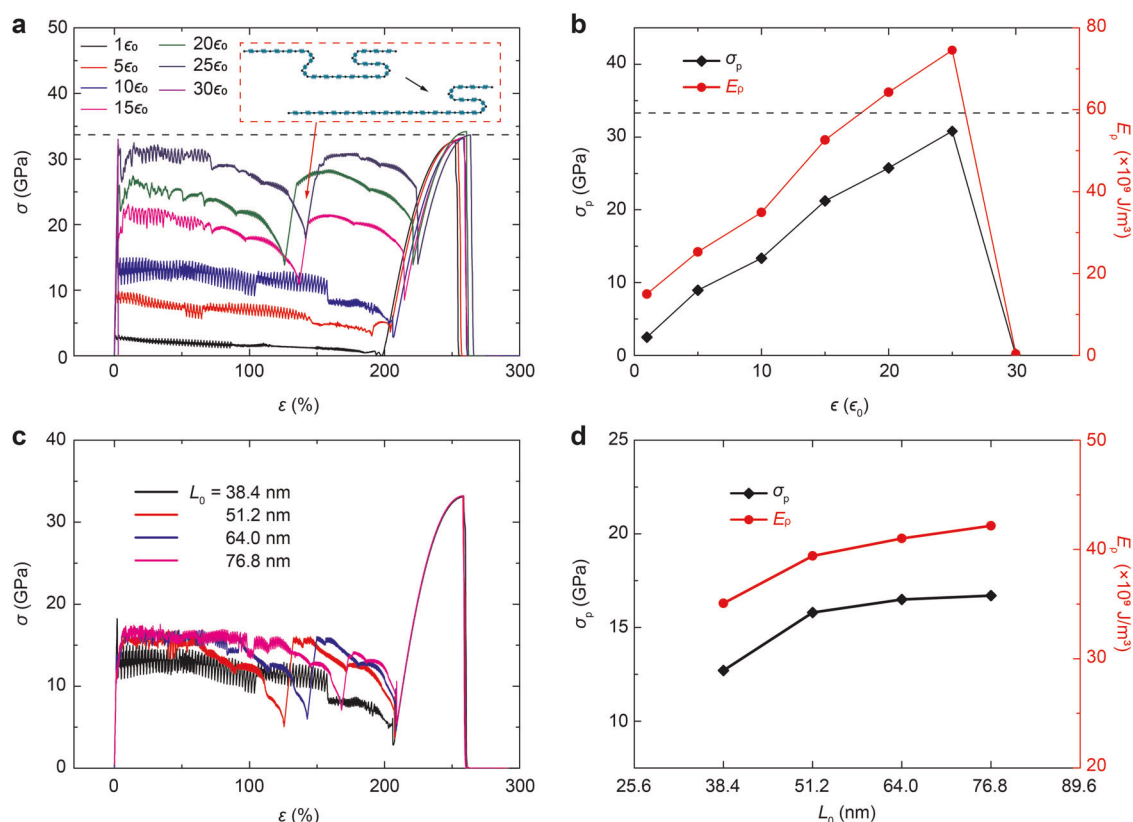


Fig. 5 Effects of mechanical and geometrical parameters on the mechanical behaviors of SFGMs. a Strain–stress curves of SFGMs having different interface interactions (ϵ_0), where the dashed line is about the upper limit of stress. **b** Effect of ϵ_0 on the key mechanical properties of SFGMs. **c** Strain–stress curves of SFGMs having different self-folded lengths (L_0). **d** Effect of L_0 on the key mechanical properties of SFGMs.

Theoretical analysis

To capture the correlation between the structure and property of SFGMs, theoretical analysis is made here. As shown in Supplementary Fig. 1, the overall loads applied on SFGM are transferred into the intralayer tensile deformation and the interlayer shear deformation. Based on the deformable tension-shear (DTS) chain model,⁴ an effective Young's modulus Y_{eff} of SFGMs can be given as

$$Y_{\text{eff}} = \frac{D}{nh_0 \{1/2 + [(1+c)/s](l_0/l_{\text{eff}})\}}, \quad (1)$$

where n is the number of self-folded layers (Supplementary Fig. 8), h_0 is the interlayer distance between adjacent folded layers, c and s

represent $\cosh(l_{\text{eff}}/l_0)$ and $\sinh(l_{\text{eff}}/l_0)$, G is the interlayer shear modulus, D is the in-plane tensile stiffness of graphene sheets, $l_0 = (Dh_0/4G)^{1/2}$ is the characteristic length in the model, and l_{eff} is the effective self-folded length considering the difference between self-folded topology of SFGMs and the staggered arrangement of sheets in DTS model, which is assumed to linearly depend on the self-folded length ($l_{\text{eff}} = f_1 L_0$, where f_1 is a pre-factor).

In addition to Y_{eff} of SFGMs, σ_1 closely correlates with σ_p and E_p , which is greatly important to determine the level of load bearing of SFGMs. Considering the two failure mechanisms as illustrated in Supplementary Fig. 9: (1) Graphene sheets are broken before the sliding and unfolding of self-folded layers, which is denoted as

mode G. (2) The interlayer of self-folded layers slides before the fracture of graphene sheets, which is denoted as mode I. Therefore, σ_1 is the lower value selected from these two failure modes, that is

$$\sigma_1 = \min \begin{cases} \frac{\sigma_s}{n} & (\text{mode G}) \\ \frac{D_{SV}\epsilon}{n(1+\epsilon)l_0} & (\text{mode I}) \end{cases}, \quad (2)$$

where σ_s is the tensile strength of monolayer graphene. In the deformation mechanism of stick-slip, the shear modulus depends linearly on the interlayer interaction ($G = f_2\epsilon$, Supplementary Fig. 4). Thus l_{eff}/l_0 can be given:

$$\frac{l_{\text{eff}}}{l_0} = f_1 L_0 \sqrt{\frac{4f_2\epsilon}{Dh_0}}. \quad (3)$$

Combining Eqs. (1)–(3) and the results of MD simulations, it is found that the prediction of σ_1 and Y_{eff} with the increasing of L_0 agrees with the simulation results (Supplementary Fig. 6a, b). Similarly, the predicted σ_1 and Y_{eff} with the increasing of ϵ are also verified by the simulation (Supplementary Fig. 6c, d). It can be found that Y_{eff} of SFGMs first increases and then converges to a limited value with the increasing of L_0 and ϵ_0 , and σ_1 of SFGMs exhibits similar evolutionary trends with the increasing of L_0 and ϵ_0 .

The above-mentioned model well predicts the mechanical behaviors of SFGMs in stage I of strain–stress curve, since the linearly elastic approximation in the model is satisfied. As the strain increases, the shear-lag model fails to predict complex mechanical behaviors, such as strain localization and interlayer unfolding. Hence, we give qualitative interpretations for stages II–IV of the strain–stress curves. In stage II, the stress first experiences a slight drop because of the transition from static to dynamic friction. Then the stress reaches a plateau because the self-folded length is saturated in this region.⁸ Finally, the stress decreases as strain increases, resulting from the decreasing of unsaturated self-folded length after excessive interlayer sliding. For stage III, the continuum mechanics-based model does not work considering the transition from the folded multilayers to unfolded monolayer, and we cannot give its constitutive relation quantitatively. For stage IV, the SFGM completely unfolds into monolayer structure, the behavior of which is similar to that of monolayer graphene.

Additional remarks

First, the tensile strength and fracture strain of SFGMs and other graphene-based materials reported in computational and experimental studies are summarized in Fig. 1. It is remarked here that the graphene-based materials fabricated in experiments possess

multi-level structures and considerable defects resulting from the fabrication process,⁵² which are difficult to directly compare with defect-free SFGMs. For example, a regular self-folded structure is considered in the previous discussion and the effects of defects in the building blocks and nonuniform functional groups have not been considered, which, however, are common microstructural structures of graphene-based materials and are responsible for the weakening of building blocks and load transfer. Meanwhile, interfacial engineering could enhance interface load transfer but weaken the intrinsic mechanical resistance of graphene building blocks. These dual roles of interfacial engineering discussed in our previous work⁸ would also exist in SFGMs if introducing interfacial engineering. In view of these facts, we expect here that the SFGMs set a reference limit on the strength–ductility of graphene-based materials and provide a guideline for the design and fabrication of graphene-based materials with high strength and ductility. With these arguments, practical SFGMs with high mechanical performance are promising to be fabricated in the future.

Second, the strength–ductility of SFGMs can be tailored by modulating the number of self-folded layers (n). For example, the SFGMs with 3, 5, and 7 self-folded layers are constructed as illustrated in Supplementary Fig. 8. The original thickness of SFGMs with n self-folded layers is about n times of that of pristine graphene. Note that the n self-folded layers would eventually unfold into one layer, and then the unfolded layer breaks down at the end of stretching SFGMs. Hence, the nominal tensile strength of SFGMs with n self-folded layers can be predicted as σ_s/n , where σ_s is the tensile strength of monolayer graphene (about 100 GPa calculated in this work). Meanwhile, the nominal fracture strain of SFGMs with n self-folded layers can be approximately predicted as $[n(1 + \epsilon_s)L_0 - L_0]/L_0 = n(1 + \epsilon_s) - 1$, where ϵ_s is the fracture strain of monolayer graphene (about 19% calculated in this work). The simulation results demonstrate that the increasing of n leads to the decreasing of tensile strength but increasing of fracture strain, which agrees substantially with the predictions (Fig. 6).

Finally, limited by the computational resources of full-atom simulations, we used a unit cell of SFGMs as the RVE to study the mechanical performance of SFGMs. To investigate the effect of RVE size, we conducted additional simulations of RVEs with large sizes by extending the unit cell of SFGMs in horizontal and vertical directions, respectively (Supplementary Fig. 10). The simulation results demonstrate that the extended RVEs have more folded parts, which make them possible to appear more unfolding signals of individual parts resulting from strain localization (inset of Supplementary Fig. 10a). Despite this difference, all folded parts in the RVEs of different sizes would eventually unfold into flat monolayer and thus break down, making their key mechanical

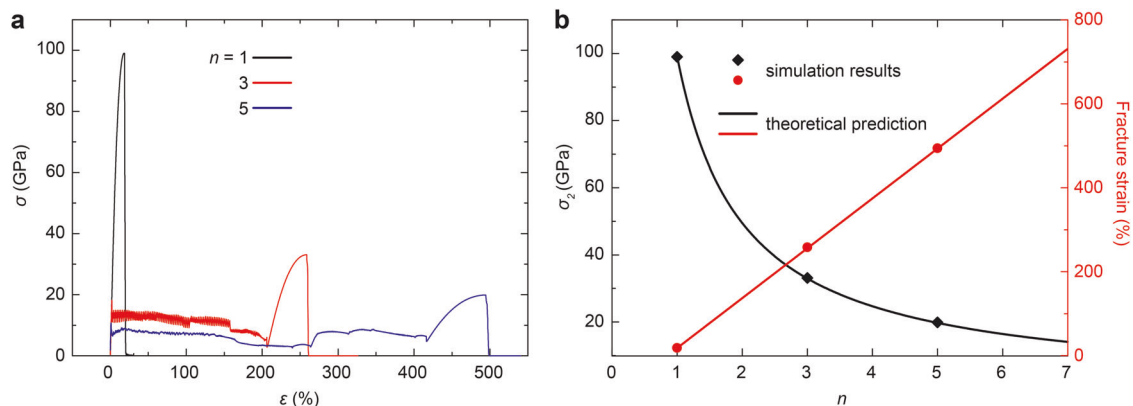


Fig. 6 Effect of the number of self-folded layers on the mechanical behaviors of SFGMs. **a** Stress–strain curves of SFGMs ($n = 1, 3,$ and 5). **b** Tensile strength and fracture strain of SFGMs from simulation (points) and prediction (lines).

properties (tensile strength, fracture strain, and strain energy density) show slight difference.

To summarize, we propose a topological strategy to enhance the mechanical properties of carbon-nanoarchitected materials by self-folding graphene into macroscopic materials and investigate the overall mechanical properties of these materials having different interface interaction and self-folded length on the basis of MD simulations and continuum model-based analysis. The optimal interface interaction and self-folded length to maximize mechanical performance of SFGMs are predicted, offering a rational guide for the design and fabrication of high-performance structural materials using carbon nanostructures as building blocks. Finally, the irregular and defective microstructures neglected in our model and the room for further optimization of SFGMs are discussed, which provide a practical insight into utilizing the bio-inspired self-folding strategy in the fabrication of graphene-based materials to break the trade-off between strength and ductility.

METHODS

To explore the mechanical responses of SFGMs to tensile loads, MD simulations of uniaxial tensile tests are carried out on the RVE of SFGMs using large-scale atomic/molecular massively parallel simulator (LAMMPS) computational package.⁵³ The adaptive intermolecular reactive empirical bond-order (AIREBO) potential⁵⁴ is adopted for its abilities to capture the deformation and failure of carbon nanostructures, such as the bond breaking and formation.^{55,56} To avoid the original overestimation of the strength of the C–C bonds, the potential cutoff is set to 2 Å.⁵⁷ In the pristine potential, the system energy is described by

$$E = \frac{1}{2} \sum_i \sum_{j \neq i} \left[E_{ij}^{\text{REBO}} + E_{ij}^{\text{LJ}} + \sum_{k \neq i, j} \sum_{l \neq i, j, k} E_{ijkl}^{\text{TOR}} \right], \quad (4)$$

where E^{REBO} , E^{LJ} and E^{TOR} are the terms of covalent bonding, interface and torsion interactions, respectively. The interface interaction is determined by E^{LJ} with LJ 12-6 form

$$V_{ij}^{\text{LJ}}(r_{ij}) = 4\epsilon \left[\left(\frac{\sigma_0}{r_{ij}} \right)^{12} - \left(\frac{\sigma_0}{r_{ij}} \right)^6 \right], \quad (5)$$

where σ_0 represents the distance between atoms as the potential energy is equal to 0 and ϵ defines the potential well. To investigate the effect of different level of interface interaction in SFGMs, the Lennard–Jones potential well of AIREBO potential is modified before SFGM sample is stretched to unfold accordingly. The Newton equations of motion are integrated using the Verlet algorithm with a time step of 0.5 fs. To avoid the size effect of the models, periodic boundary conditions along three dimensions are used in the simulations. Before the tensile deformation protocol is started, all constructed structures of SFGMs are fully energy minimized using a conjugate gradient algorithm. Afterwards, mechanical responses to tensile loads of these structures are investigated at 0.1 K using a Nosé–Hoover thermostat with a characteristic relaxation time of 0.1 ps. We also perform simulations of SFGMs under finite temperature of 300 K to study the effect of thermal fluctuation on the stability, deformation mechanism as well as mechanical properties of SFGMs. First, simulations of SFGMs with different L_0 and ϵ under the temperature of 300 K are conducted for 1 ns, which demonstrate that the stability of SFGMs increases with increasing of L_0 and ϵ (Fig. 3). Furthermore, mechanical tests of SFGMs are conducted under the temperatures of 0.1 and 300 K, respectively (Supplementary Fig. 11). Compared with that of SFGMs tested under the temperature of 0.1 K, the stick-slip peaks of SFGMs during interlayer sliding process (stage II) under finite temperature of 300 K are reduced, which could be attributed to that the thermal fluctuation helps SFGM to overcome the energy barrier for interlayer sliding, while the tensile strength, fracture strain, and strain energy density of SFGMs exhibit slight difference, suggesting the minor effect of finite temperature of 300 K on the key mechanical properties of SFGMs. The uniaxial tensile strain is applied by uniaxially deforming the periodic simulation box and applying affine displacement to the atomic positions until the failure of structures, in which the other two transverse directions are equilibrated of 1 bar by coupling to a Berendsen barostat. We did a convergence test on deformation velocities, which demonstrates that the deformation velocity

of 20 m/s has a slight effect on the key mechanical performance of SFGMs (Supplementary Fig. 3). Thus, this deformation velocity is adopted, which represents a good balance between computational accuracy and efforts.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

CODE AVAILABILITY

All codes of this current study are available from the corresponding author upon reasonable request.

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AUTHOR CONTRIBUTIONS

E.G. conceived the idea. Z.L. provided advices on this work. X.J. and E.G. carried out the simulation and related data analysis. All authors participated in the writing of the manuscript.

COMPETING INTERESTS

The authors declare no competing interests.

ADDITIONAL INFORMATION

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Supplementary Information for

Bio-inspired self-folding strategy to break the trade-off between strength and ductility in graphene-based materials

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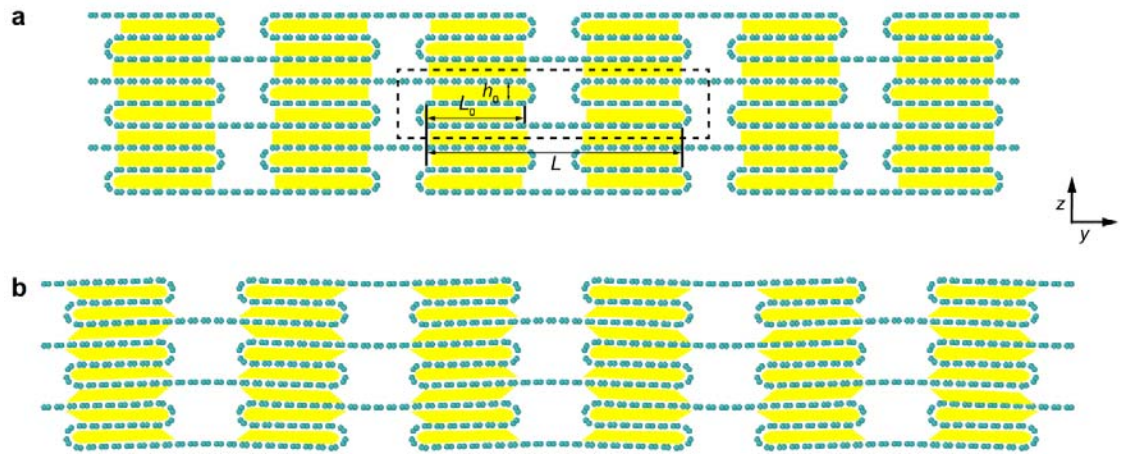
*Corresponding author. Email: enlaigao@whu.edu.cn.

The Supplementary Information contains

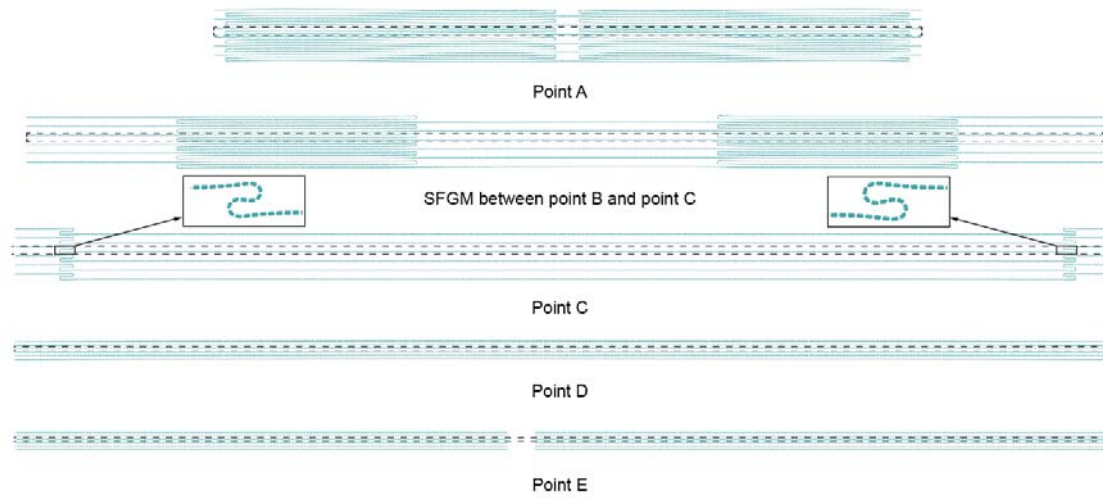
- Supplementary Table 1.
- Supplementary Figures 1-11.

Supplementary Table 1 Tensile strength and strain to failure of graphene-based materials reported in literatures, as compared with that of rubber and carbon fiber.

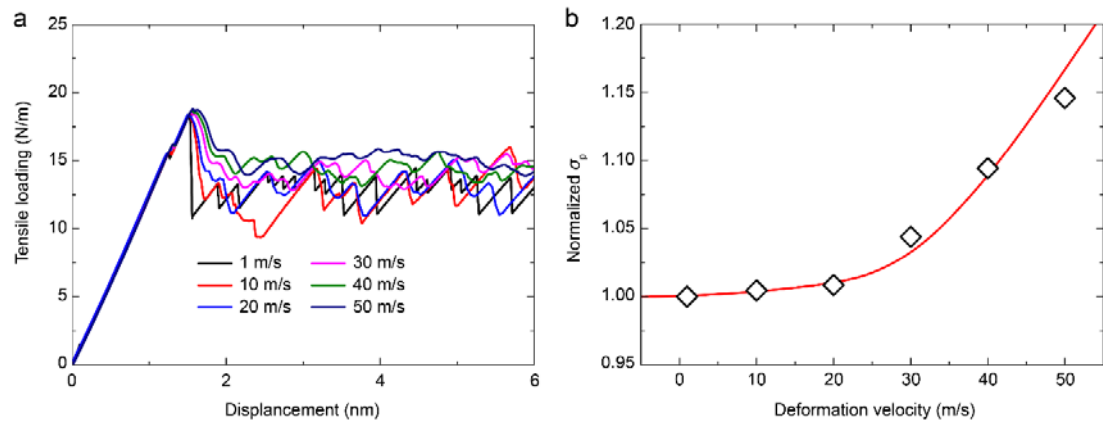
Species	Tensile strength (MPa)	Strain to failure (%)	Refs.
Graphene Film	1,054.2	6.6	1
Graphene Film	944.5	5.9	2
Graphene Film	765	6.2	3
Graphene Film	28.2	23	4
Graphene Oxide Fiber (GOF)	102	6.8-10.1	5
Graphene Fiber (GF)	300	5.5	6
GF	~555	3.5-5.6	7
GOF	452 ± 24	4.5-5.4	8
GF	162	1.7-3.0	9
GF	~500	~3.0	10
GF	238	2.2	11
GOF	6.9	4.6	12
Reduced GOF (RGOF)	11.1	6.2	13
RGOF	180	4.2	13
RGOF	197	4.2	14
RGOF	84	3.3	14
GOF	33.2	1.6	15
RGOF	383	1.0	15
GOF	31.1	78.6	16
RGOF	39.2	1.5	16
GOF	240	5-6	17
RGOF	360.1 ± 12.7	~2.5	18
GF	125 ± 10	~3.7	19
GF	1080	1.45	20
GF	1450	0.53	21
GF	1900	0.65	22



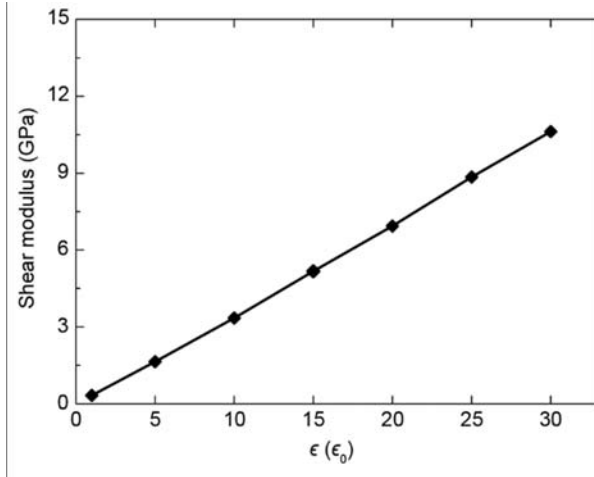
Supplementary Figure 1. Structures of SFGM. (a) Illustration of SFGMs before and (b) after stretching, where the cyan and yellow represent the intralayer and interlayer medium of SFGMs, respectively.



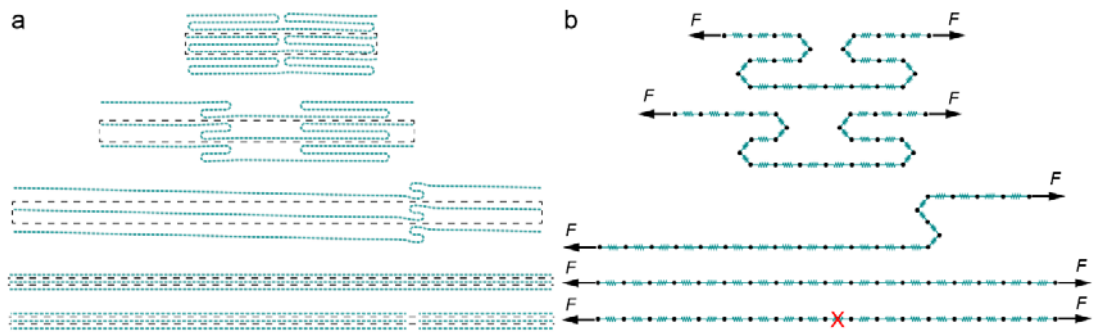
Supplementary Figure 2. MD snapshots of SFGM under tension, which correspond to the points of A, B, C, D, and E in strain-stress curve of **Fig. 4**, respectively. The region in black dashed line is the RVE of SFGM.



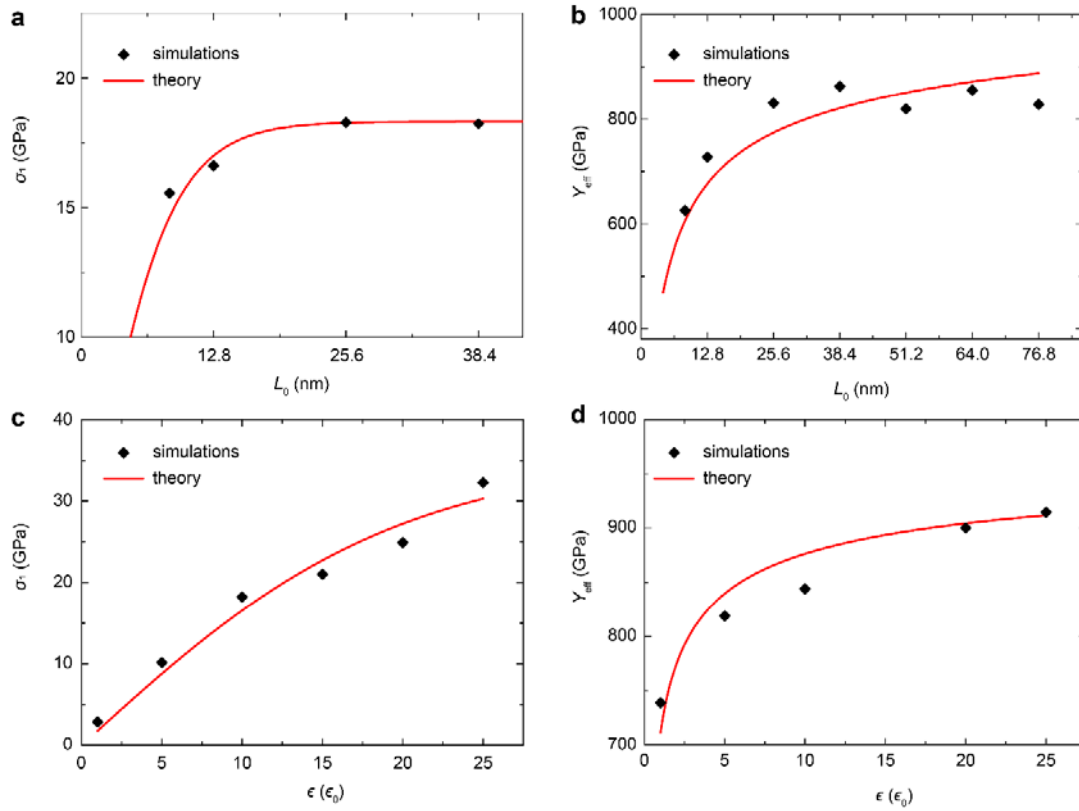
Supplementary Figure 3. (a) Relationship between tensile loading (tensile force per width) and displacement of SFGMs under various deformation velocities. (b) σ_p of SFGMs loaded using different deformation velocities, which is normalized by the σ_p at deformation velocity of 1 m/s.



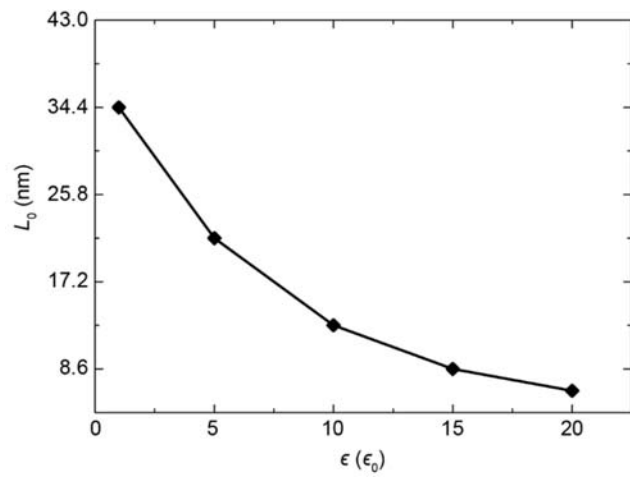
Supplementary Figure 4. Relation between ϵ and shear modulus (G).



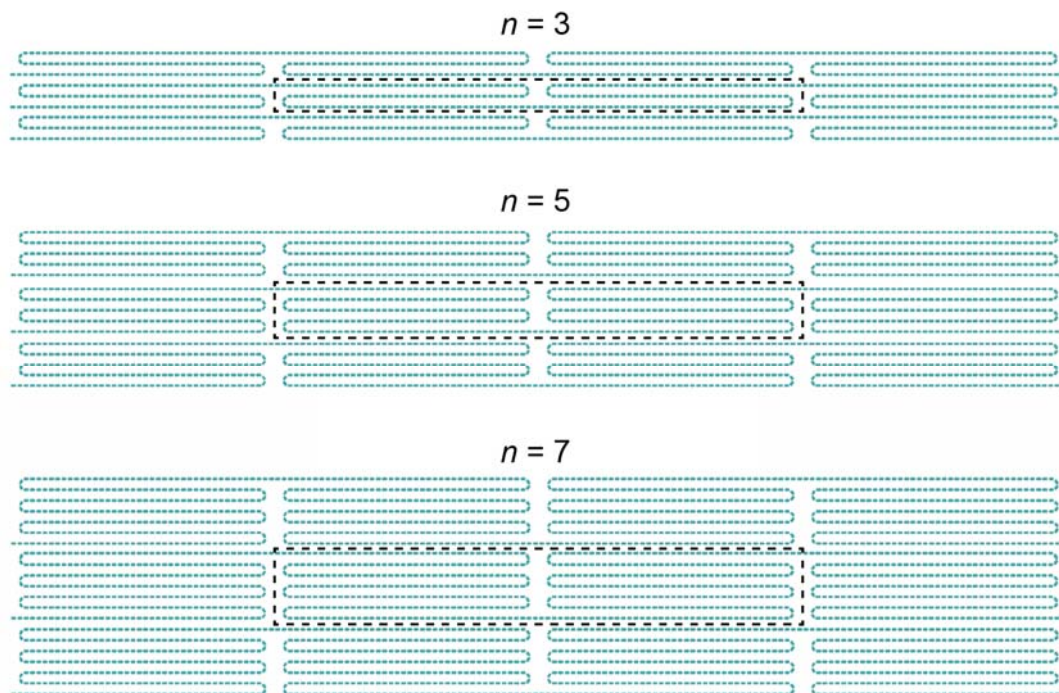
Supplementary Figure 5. (a) MD snapshots and (b) illustrated cartoons of asymmetrically unfolded SFGM.



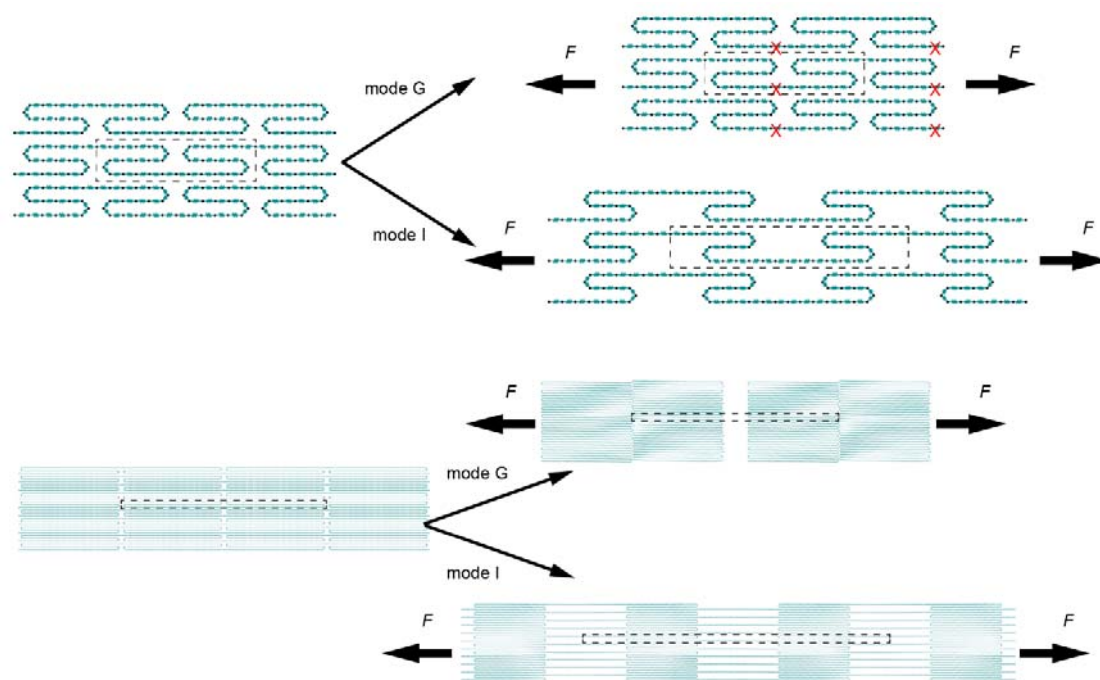
Supplementary Figure 6. (a-b) σ_1 and Y_{eff} of SFGMs as the functions of L_0 . (c-d) σ_1 and Y_{eff} of SFGMs as the functions of ϵ .



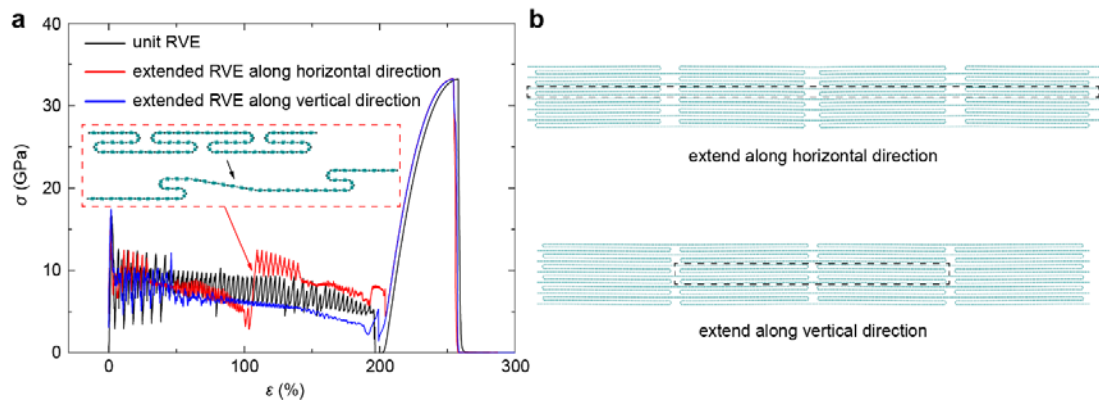
Supplementary Figure 7. Optimal self-folded length decreases with the increasing of ϵ .



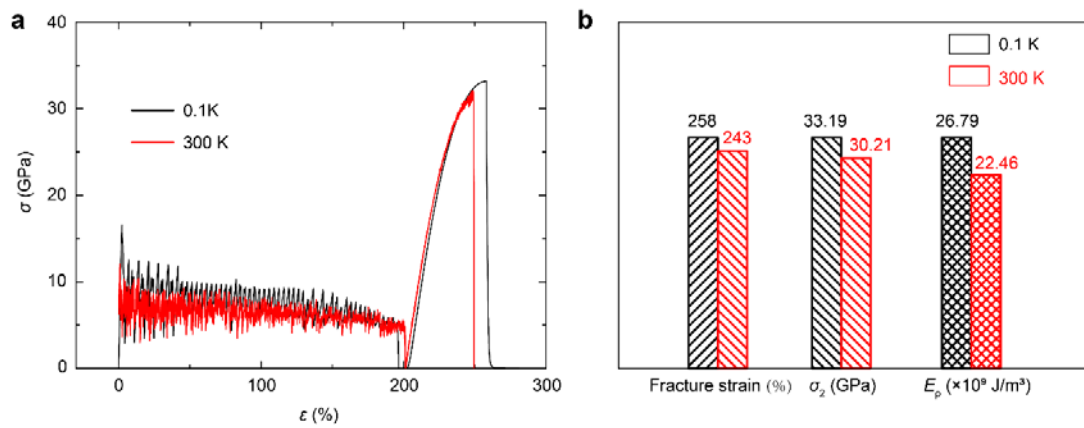
Supplementary Figure 8. SFGMs with different numbers of self-folded layers ($n = 3, 5, 7$).



Supplementary Figure 9. Illustrated cartoons and MD snapshots of the two failure modes (intralayer failure before sliding of SFGMs and interlayer sliding to unfold SFGMs).



Supplementary Figure 10. (a) Strain-stress curves of unit RVE and extended RVEs. (b) Structures of the extended RVEs.



Supplementary Figure 11. (a) Strain-stress curves and (b) key mechanical properties of SFGMs under the temperature of 0.1 K and 300 K, respectively.

Supplementary References

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